

Show all work on these pages and circle your answers. Read the instructions for each set of questions, and have fun ☺

Provide a short description for the following:

1) What is a removable discontinuity? _____

2) What is a non-removable discontinuity? _____

Multiply or divide as indicated. State any restrictions.

$$3) \frac{x^2-2x-24}{x^2+7x+12} \div \frac{x-6}{x^2-1}$$

$$\frac{(\cancel{x-6})(x+4)}{(x+3)(x+4)} \cdot \frac{(x-1)(x+1)}{\cancel{x-6}}$$

$$\frac{(x-1)(x+1)}{x+3}, x \neq \{-3, -4, 6\}$$

$$4) \frac{x^2-1}{5x-5} \times \frac{10}{3x^2+6x+3}$$

$$\frac{(\cancel{x+1})(\cancel{x-1})}{5(\cancel{x-1})} \cdot \frac{10}{3(x+1)(x+1)}$$

$$\frac{2}{3(x+1)}, x \neq \pm 1$$

Add or subtract as indicated. State any restrictions.

$$5) \frac{x-7}{x^2+4x-5} - \frac{x-9}{x^2+3x-10}$$

$$\frac{(x+5)(x-1)}{(x-2)} - \frac{(x+5)(x-2)}{(x-1)}$$

$$\frac{x^2-9x+14 - (x^2-10x+9)}{(x+5)(x-1)(x-2)}$$

$$\frac{\cancel{x^2}-9x+14-\cancel{x^2}+10x-9}{(x+5)(x-1)(x-2)}$$

$$6) \frac{3x}{x^2-4} + \frac{6}{x+2} \cdot \frac{x-2}{x-2}$$

$$\frac{(x+2)}{(x-2)}$$

$$\frac{3x + 6x - 12}{(x+2)(x-2)} = \frac{9x-12}{(x+2)(x-2)}$$

$$x \neq \pm 2$$

$$\Rightarrow \frac{x+5}{(x+5)(x-1)(x-2)}, x = \{-5, 1, 2\}$$

~more~

Solve for x. State any restrictions.

$$\frac{2 \cdot 3 \cdot 3 \cdot 2 \cdot 8}{9 \cdot 12}$$

$$7) \frac{1}{x} + \frac{x}{8} = \frac{18}{8}$$

$$\begin{aligned} 3x + x^2 &= 108 \\ x^2 + 3x - 108 &= 0 \\ (x + 12)(x - 9) &= 0 \\ x &= \{-12, 9\} \end{aligned}$$

$$8) \frac{2}{x+3} - \frac{1}{x} = \frac{-6}{x(x+3)}$$

$$2x - x - 3 = -6$$

$$x = -3, \leftarrow \text{restricted}$$

NO SOLUTION

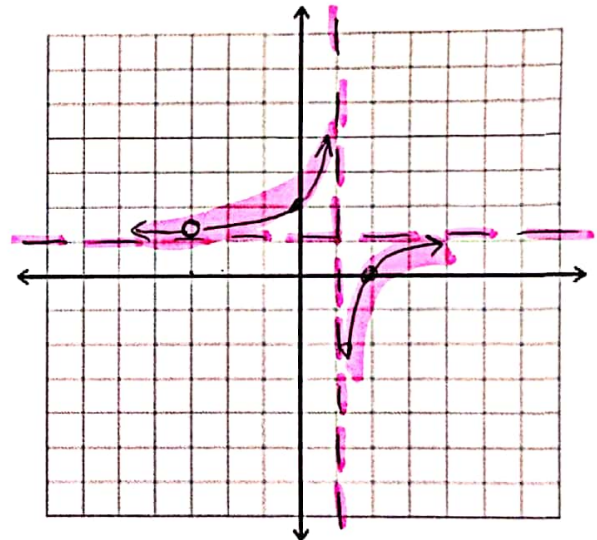
For each of the following find the vertical asymptotes, horizontal asymptotes, and holes if they exist. Sketch the graph.

$$9) y = \frac{(x+3)(x-2)}{(x+3)(x-1)}$$

vertical asymptote $x = 1$

horizontal asymptote $y = 1$

hole $(-3, \frac{5}{4})$

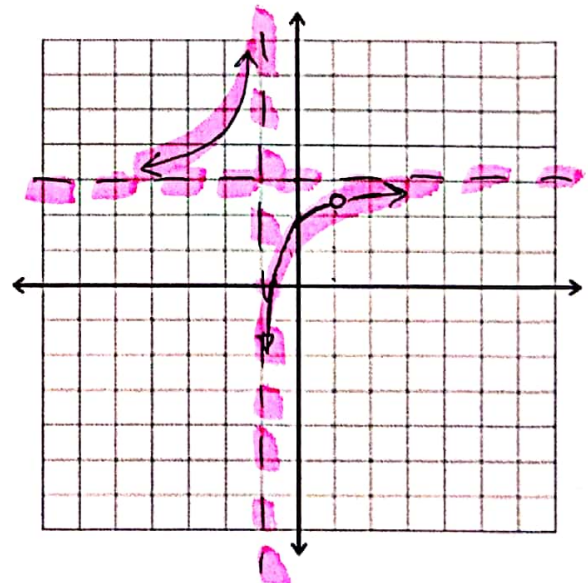


$$10) f(x) = \frac{3x^2 - x - 2}{x^2 - 1} \cdot \frac{(3x+2)(x-1)}{(x+1)(x-1)}$$

vertical asymptote $x = -1$

horizontal asymptote $y = 3$

hole $(1, \frac{5}{2})$



~more~

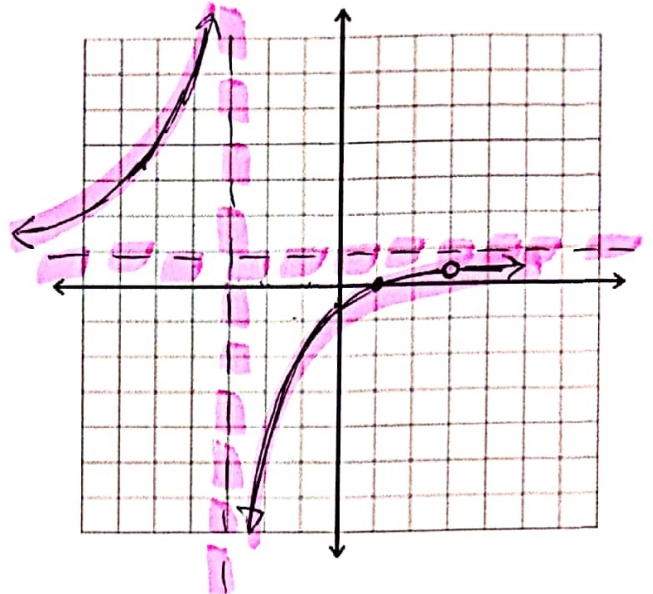
For each of the following find the vertical asymptotes, horizontal asymptotes, and holes if they exist. Sketch the graph.
(continued)

$$11) f(x) = \frac{x^2 - 4x + 3}{x^2 - 9} = \frac{(x-3)(x-1)}{(x-3)(x+3)}$$

vertical asymptote $x = -3$

horizontal asymptote $y = 1$

hole $(3, 1/3)$



Give a possible rational function, $f(x)$, that ...

- 12) ... has a hole at $x=5$, and a vertical asymptote at $x=-2$ (make one up).

$$f(x) = \frac{(x-5)(3)}{(x-5)(x+2)}$$

Sample
←

~end~