

Ch 6 Test

Simplify each radical expression.

1. $\sqrt{81x^6y^{10}}$
 $\sqrt{81} \sqrt{x^6} \sqrt{y^{10}}$
 $9x^3y^5$

2. $\sqrt[3]{27y^{12}}$
 $\sqrt[3]{27} \sqrt[3]{y^{12}}$
 $3y^4$

3. $\sqrt[4]{625x^{16}}$
 $\sqrt[4]{625} \sqrt[4]{x^{16}}$
 $5x^4$

Multiply and simplify.

4. $\sqrt{3x^7} \sqrt{21x}$
 $\sqrt{3 \cdot 21 \cdot x^7 \cdot x}$
 $\sqrt{63 \cdot x^8}$
 $\sqrt{9} \sqrt{7} \sqrt{x^8}$
 $3x^4\sqrt{7}$

5. $\sqrt[3]{6x^3} \sqrt[3]{9x^7}$
 $\sqrt[3]{54x^8}$
 $\sqrt[3]{27 \cdot 2 \cdot x^6 \cdot x^2}$
 $3x^2 \sqrt[3]{2x^2}$

Rationalize each denominator. Simplify your answer

6. $\frac{\sqrt{x}}{\sqrt{11}} \cdot \frac{\sqrt{11}}{\sqrt{11}}$
 $\frac{\sqrt{11x}}{11}$

7. $\frac{\sqrt[3]{7}}{\sqrt[3]{3x^2}} \cdot \frac{\sqrt[3]{3x^2}}{\sqrt[3]{3x^2}} \cdot \frac{\sqrt[3]{3x^2}}{\sqrt[3]{3x^2}}$

$\frac{\sqrt[3]{83x^4}}{3x^2} = \frac{\sqrt[3]{63x}}{3x^2}$

$\frac{\sqrt[3]{63x}}{3x}$

Multiply. Express the product in polynomial form.

8. $(3 + \sqrt{7})^2$

$$9 + 6\sqrt{7} + 7$$

$$16 + 6\sqrt{7}$$

9. $(4 + \sqrt{5})(3 - \sqrt{5})$

$$12 - 4\sqrt{5} + 3\sqrt{5} - 5$$

$$7 - \sqrt{5}$$

Simplify.

10. $81^{\frac{3}{4}}$

$$(81^{1/4})^3$$

$$(3)^3$$

$$27$$

11. $25^{\frac{3}{2}}$

$$(25^{1/2})^3$$

$$(5)^3$$

$$125$$

Write each expression in simplest form.

12. $(x^{\frac{5}{2}})^4$

$$x^{\frac{5}{2} \cdot \frac{4}{1}}$$

$$x^{10}$$

13. $(x^{\frac{5}{6}}y^{\frac{1}{4}})^{12}$

$$x^{(\frac{5}{6})(12)} y^{(\frac{1}{4})(12)}$$

$$x^{10} y^3$$

Solve.

14. $\sqrt{2x+5} = 11$
 $2x+5 = 121$
 $2x = 116$
 $x = 58$

15. $(x-7)^{\frac{2}{3}} = 36$
 $\left[(x-7)^{\frac{2}{3}}\right]^{\frac{3}{2}} = (36)^{\frac{3}{2}}$
 $x-7 = 216$
 $x = 223$

Let $f(x) = x + 7$ and $g(x) = 3 - x$. Perform the operations, simplify, & state any restrictions

16. $(f-g)(x)$
 $x+7-3+x$
 $2x+4$

17. $(f \cdot g)(x) (x+7)(3-x)$
 $3x - x^2 + 21 - 7x$
 $-x^2 - 4x + 21$

18. $\left(\frac{f}{g}\right)(x) \frac{x+7}{3-x}$
 $\frac{x+7}{3-x}, x \neq 3$

Let $f(x) = 5x - 1$ and $g(x) = x^2 + 4$. Find each value or expression.

19. $(f \circ g)(x)$
 $5(x^2+4)-1$
 $5x^2+20-1$
 $5x^2+19$

20. $(g \circ f)(3)$
 $(5x-1)^2+4$
 $25x^2-10x+1+4$
 $(g \circ f)(x) = 25x^2-10x+5$
 $25(9)-10(3)+5$
 $225-30+5$
 $\rightarrow 200 \leftarrow$